

The latest results, and photoproduction of hypernuclei in the (latest version) QMC model (and some recent other results)

K. Tsushima (JLab)

P.A.M. Guichon, V. Guzey,
R. Shyam, A.W. Thomas

NPA 814, 66 (2008): (PGTT)
arXiv:0812.1547 [nucl-th]: (STT)
arXiv:0806.3288 [nucl-th]: (VGTT)

The QMC model

P.A.M. Guichon, PLB 200, 235 (1988)

(For a review, PPNP 58, 1 (2007))

Light (u,d) quarks interact self-consistently with mean σ and ω fields

$$m^*q = m_q - g_\sigma^q \sigma = m_q - V_\sigma^q$$

\Downarrow nonlinear in σ

$$M^*_N \cong M_N - g_{\sigma\sigma}^N \sigma + (d/2)(g_{\sigma\sigma}^N)^2$$

$$\langle \sigma \rangle$$

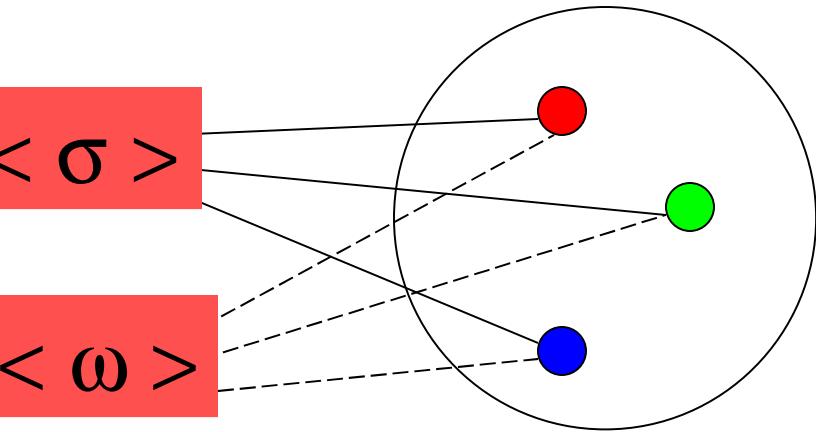
$$\langle \omega \rangle$$

$$[i \partial \cdot \gamma - (m_q - V_\sigma^q) + \gamma_0 V_\omega^q] q = 0$$

$$M^*_N = M_N - V_\sigma^N$$

$$[i \partial \cdot \gamma - (M_N - V_\sigma^N) + \gamma_0 V_\omega^N] N = 0$$

$$V_\omega^N = 3 V_\omega^q$$



Outline

- Introduction, the QMC model, finite nuclei
 - Hypernuclei in the latest QMC model (Σ, Λ)
 - Photoproduction of Λ -hypernuclei
 - Discussion, outlook for hypernuclei
5. Medium effect on GPD (informal!)
6. Speculations!!

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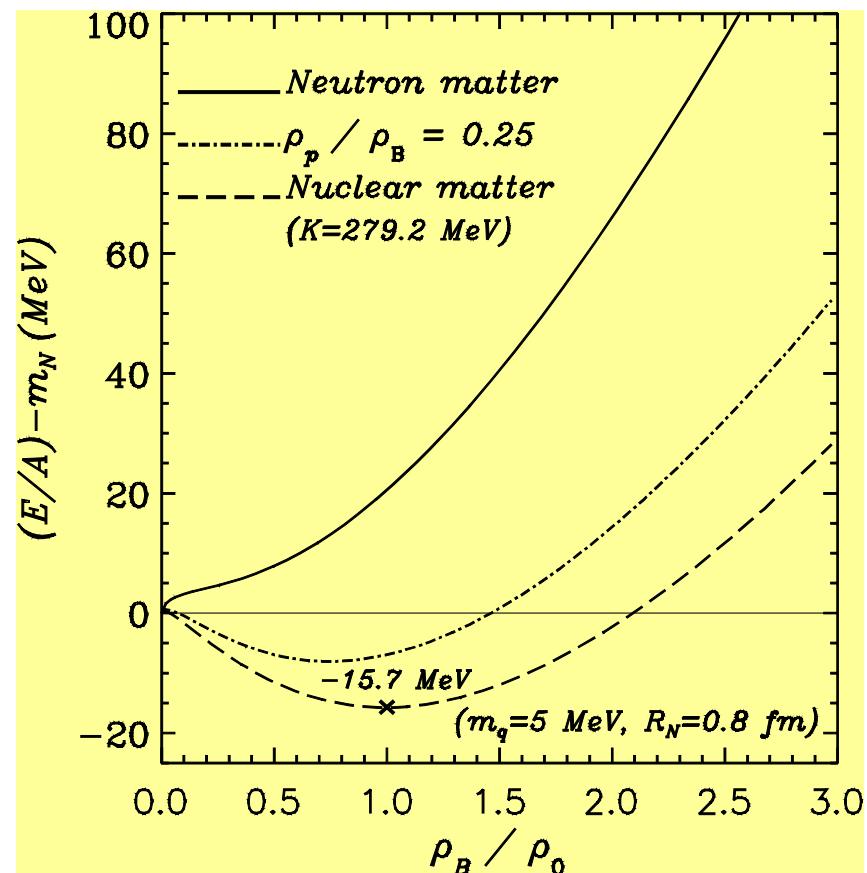
Nuclear (Neutron) matter, E/A

New saturation mechanism !

Incompressibility

$K \approx 280 \text{ MeV}$
 $(200 \sim 300 \text{ MeV})$

PLB 429, 239 (1998)



Finite nuclei (^{208}Pb energy levels)

NPA 609, 339 (1996)

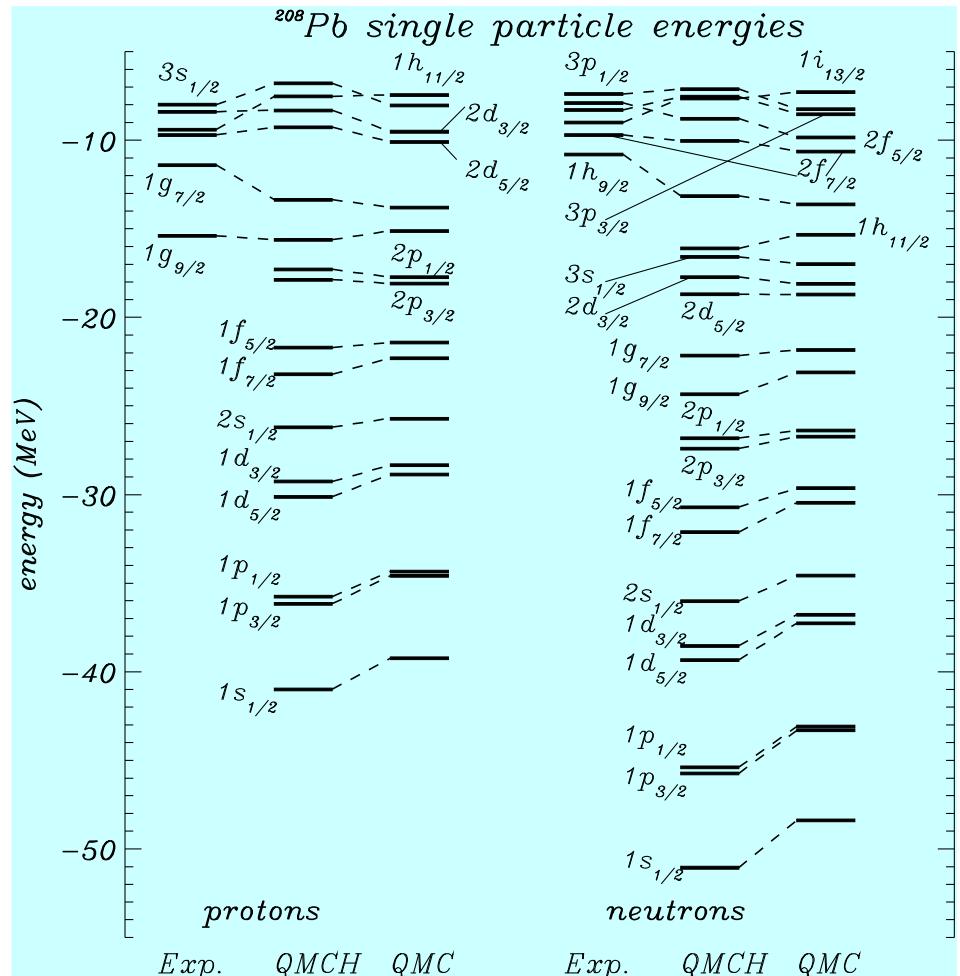
Large mass nuclei

Based on the quarks !



Hypernuclei

(the latest version of QMC)



The latest QMC model

NPA 814, 66 (2008) (arXiv:0712.1925 [nucl-th])

- Color “Coulomb-spike” effect on **OGE** hyperfine interaction (s-quark different)
(T. Barnes, PRD 30, 1961 (1984))
- \Rightarrow Smaller α_c in the MIT bag model
(PRD 12, 2060 (1976): $0.55 \rightarrow \sim 0.45$)
- **Self-consistent** inclusion in matter
 - \Rightarrow extra repulsion for Σ relative to Λ
 - \Rightarrow No Σ nuclear bound state!!

Bag mass and mag. HFC contribution (OGE)

T. DeGrand *et al.*, PRD 12, 2060 (1975)

$$M = [N_q \Omega_q + N_s \Omega_s]/R - Z_0/R + 4\pi B R^3/3$$
$$+ \Delta E_M (f) \quad (f=N, \Delta, \Sigma, \Lambda, \Xi \dots)$$

$$\Delta E_M = -3\alpha_c \sum_{a, i < j} \lambda_i \lambda_j \vec{\sigma}_i \cdot \vec{\sigma}_j [(\mu_i \mu_j)/R^3] I_{ij}$$

$$\mu_i(R), I_{ij} \longrightarrow T. DeGrand *et al.*, PRD 12, 2060 (1975)$$

(typos !)

Octet and Decuplet masses (GeV)

NPA 814, 66 (2008) (arXiv:0712.1925 [nucl-th])

Fs	ms	Λ	Σ	Ξ	Σ^*	Ξ^*	Ω
1	0.341	1.135	1.176	1.355	1.416	1.599	1.784
0.726	0.297	1.107	1.189	1.325	1.368	1.507	1.654
Exp.		1.116	1.193	1.318	1.385	1.533	1.672

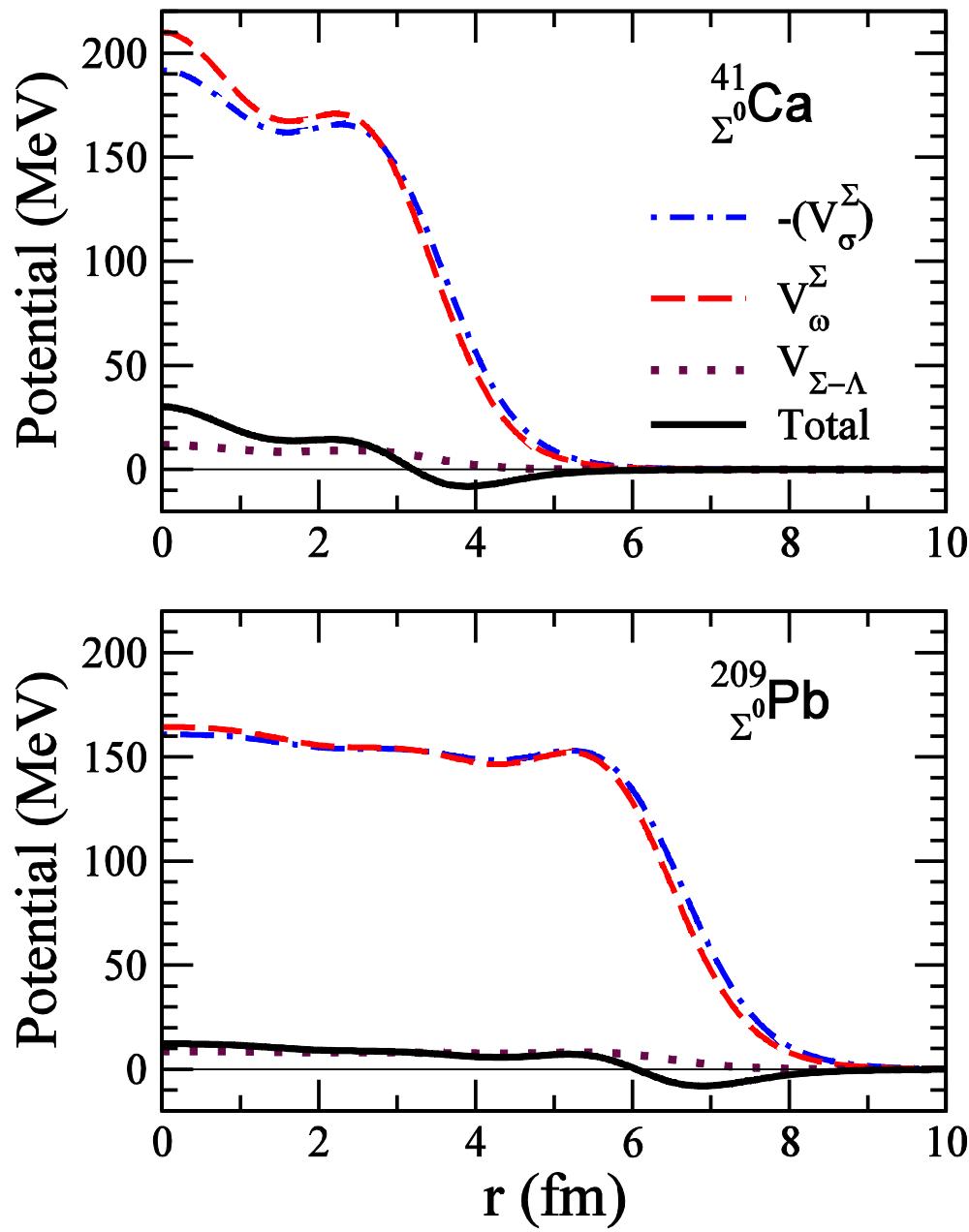
$R_N=0.8$ fm, N, Δ masses $\rightarrow B=0.5541$ fm $^{-1}$, $Z_0=2.6422$,

$\alpha_c = 0.4477$, (0.55), Less enhanced the “Coulomb-spike” for s quark
 \Rightarrow independent, Fs, ms : fit to Λ, Σ, Ξ masses (predictions)

Σ^0 potentials ($1s_{1/2}$)

Repulsion
in center
Attraction
in surface
No Σ nuclear
bound state!

HF couplings for
hyperons \Leftrightarrow
successful for high
density neutron star
(NPA 792, 341 (2007))



Hypernuclei spectra 1

NPA 814, 66 (2008) (arXiv:0712.1925 [nucl-th])

	$^{16}_{\Lambda}\text{O}$ Exp.	$^{17}_{\Lambda}\text{O}$	$^{17}_{\Xi^0}\text{O}$	$^{40}_{\Lambda}\text{Ca}$ Exp.	$^{41}_{\Lambda}\text{Ca}$	$^{41}_{\Xi^0}\text{Ca}$	$^{49}_{\Lambda}\text{Ca}$	$^{49}_{\Xi^0}\text{Ca}$
$1s_{1/2}$	-12.4	-16.2		-5.3	-18.7	-20.6	-5.5	-21.9
$1p_{3/2}$			-6.4			-13.9	-1.6	-15.4
$1p_{1/2}$	-1.85	-6.4				-13.9	-1.9	-15.4
$1d_{5/2}$						-5.5		-7.4
$2s_{1/2}$						-1.0		-3.1
$1d_{3/2}$						-5.5		-7.3

Hypernuclei spectra 2

NPA 814, 66 (2008) (arXiv:0712.1925 [nucl-th])

	$^{89}_{\Lambda}$ Yb Exp.	$^{91}_{\Lambda}$ Zr	$^{91}_{\Xi^0}$ Zr	$^{208}_{\Lambda}$ Pb Exp.	$^{209}_{\Lambda}$ Pb	$^{209}_{\Xi^0}$ Pb
$1s_{1/2}$	-23.1	<u>-24.0</u>	-9.9	-26.3	<u>-26.9</u>	-15.0
$1p_{3/2}$		<u>-19.4</u>	-7.0		<u>-24.0</u>	-12.6
$1p_{1/2}$	-16.5	<u>-19.4</u>	-7.2	-21.9	<u>-24.0</u>	-12.7
$1d_{5/2}$	-9.1	<u>-13.4</u>	-3.1	-16.8	<u>-20.1</u>	-9.6
$2s_{1/2}$		<u>-9.1</u>	—		<u>-17.1</u>	-8.2
$1d_{3/2}$	(-9.1)	<u>-13.4</u>	-3.4	(-16.8)	<u>-20.1</u>	-9.8

Summary: hypernuclei

- The latest version of QMC (OGE color Coulomb “spike” effect included self-consistently in matter) \Rightarrow
 $\forall \Lambda$ single-particle energy $1s_{1/2}$ in Pb is -26.9 MeV
(Exp. -26.3 MeV) \Leftarrow no extra parameter!
 - Small spin-orbit splittings for the Λ
 - No Σ nuclear bound state !!
- $\forall \Xi$ is expected to form nuclear bound state

Photoproduction of Λ Hypernuclei

R. Shyam, KT, A.W. Thomas, arXiv:0812.1547 [nucl-th]

Λ and K^+ are produced via s-channel

N^* excitation (dominant)

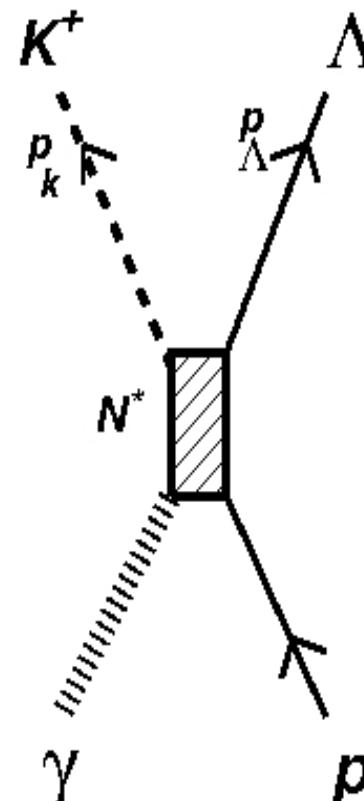
$S_{11}(1650)$, $P_{11}(1710)$

$P_{13}(1720)$

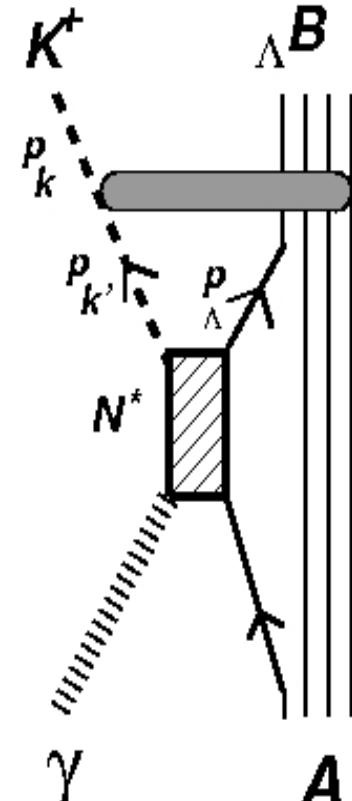
\Updownarrow

Energy region of interests,
hypernuclei production

(~ 10 % ambiguity due to
the other background \Rightarrow)



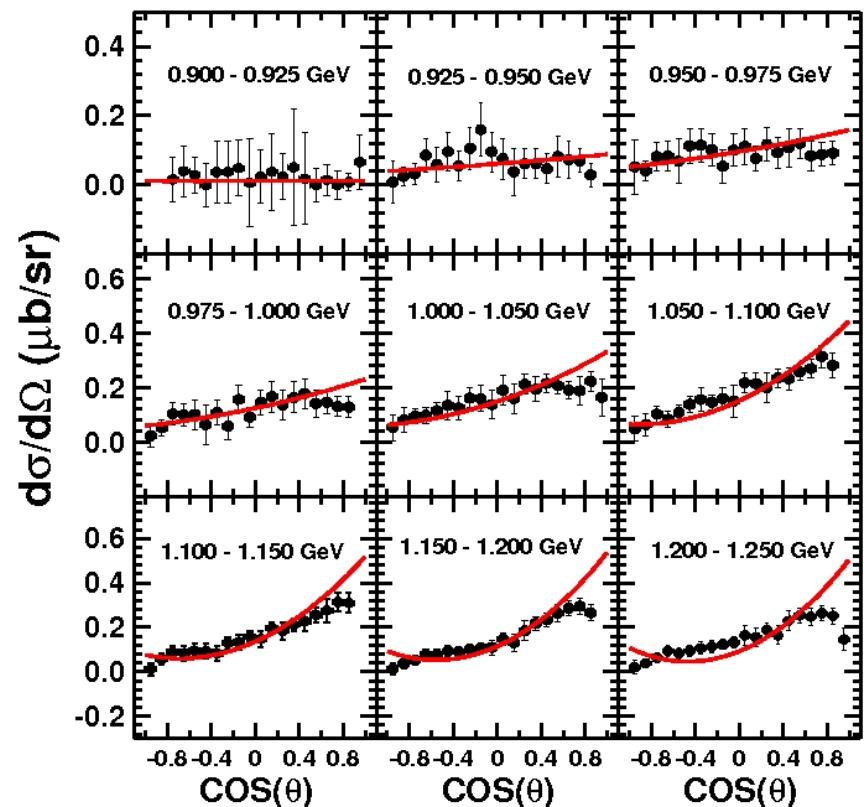
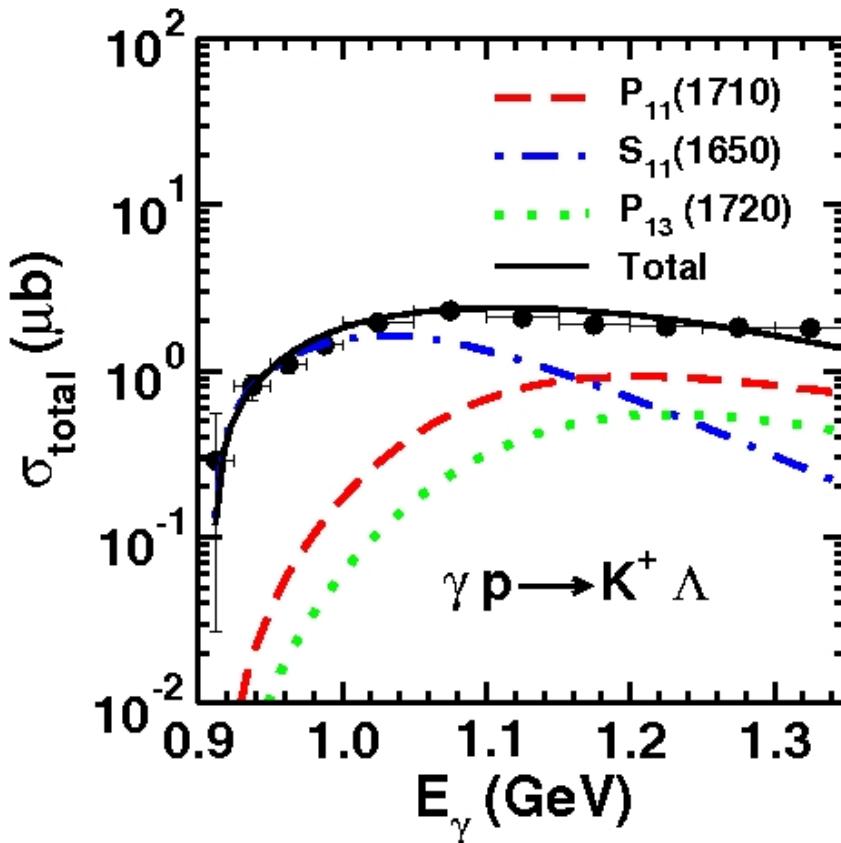
(a)



(b)

Elementary γ p \rightarrow K $^+$ Λ reaction

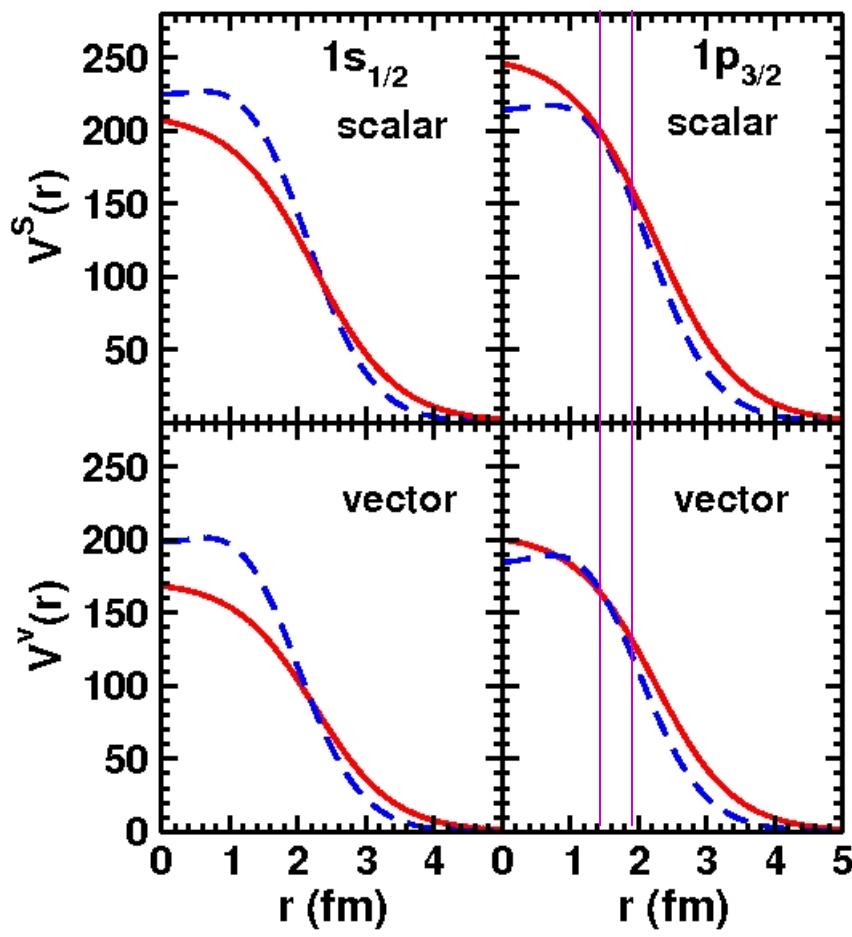
R. Shyam, KT, A.W. Thomas, arXiv:0812.1547 [nucl-th]



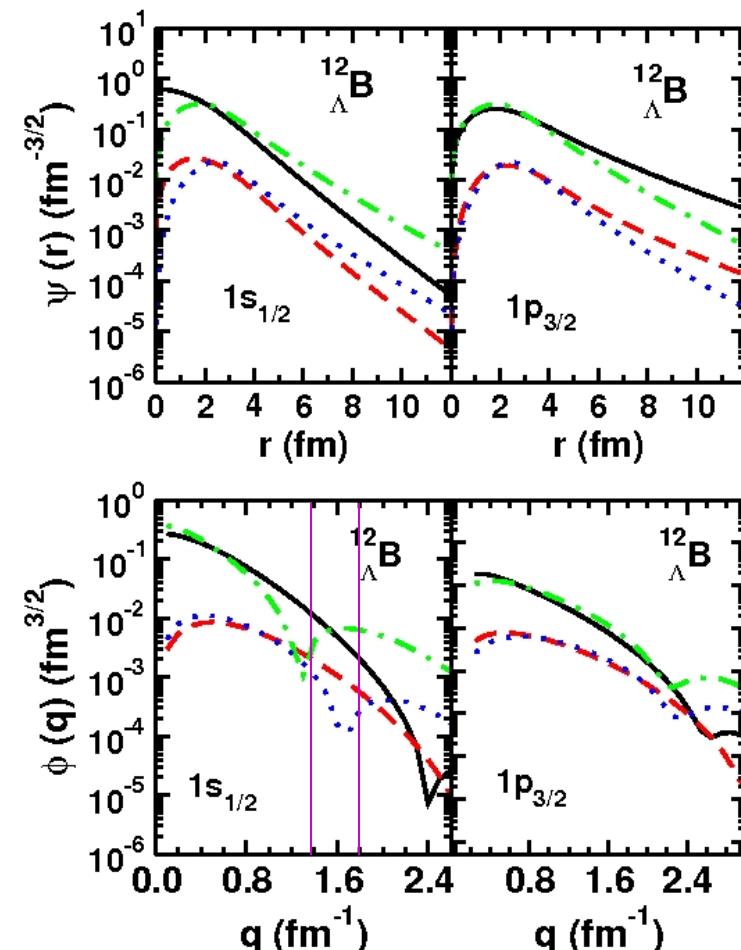
$^{12}_{\Lambda}\text{B}$ hypernuclei (MeV)

State	Exp.	QMC	V _v (W.S.)	V _s (W.S.)
$^{12}_{\Lambda}\text{B}1s_{1/2}$	11.37	14.93	171.78	-212.69
$^{12}_{\Lambda}\text{B}1p_{3/2}$	1.73	3.62	204.16	-252.28
$^{12}_{\Lambda}\text{B}1p_{1/2}$	1.13	3.62	227.83	-280.86
$(p1p_{3/2})^{-1}$ ^{12}C	15.96 Sep. energy	(\cong OK)	382.60	-472.34

Potentials and wave functions



QMC, W.S. type



|QMCU|, |QMCL|, |DiracpU|, |DiracpL|

Differential cross sections: $^{12}\text{C}(\gamma, \text{K}^+)_{\Lambda}^{12}\text{B}$

arXiv:0812.1547 [nucl-th]

$E_{\text{th}} \sim 695 \text{ MeV}$

$d\sigma/d\Omega$ at

Kaon angle $\theta = 10^\circ$

$1^-, 2^- \Leftrightarrow (1p_{3/2}, 1s_{1/2})$

(wave functions!) \Rightarrow

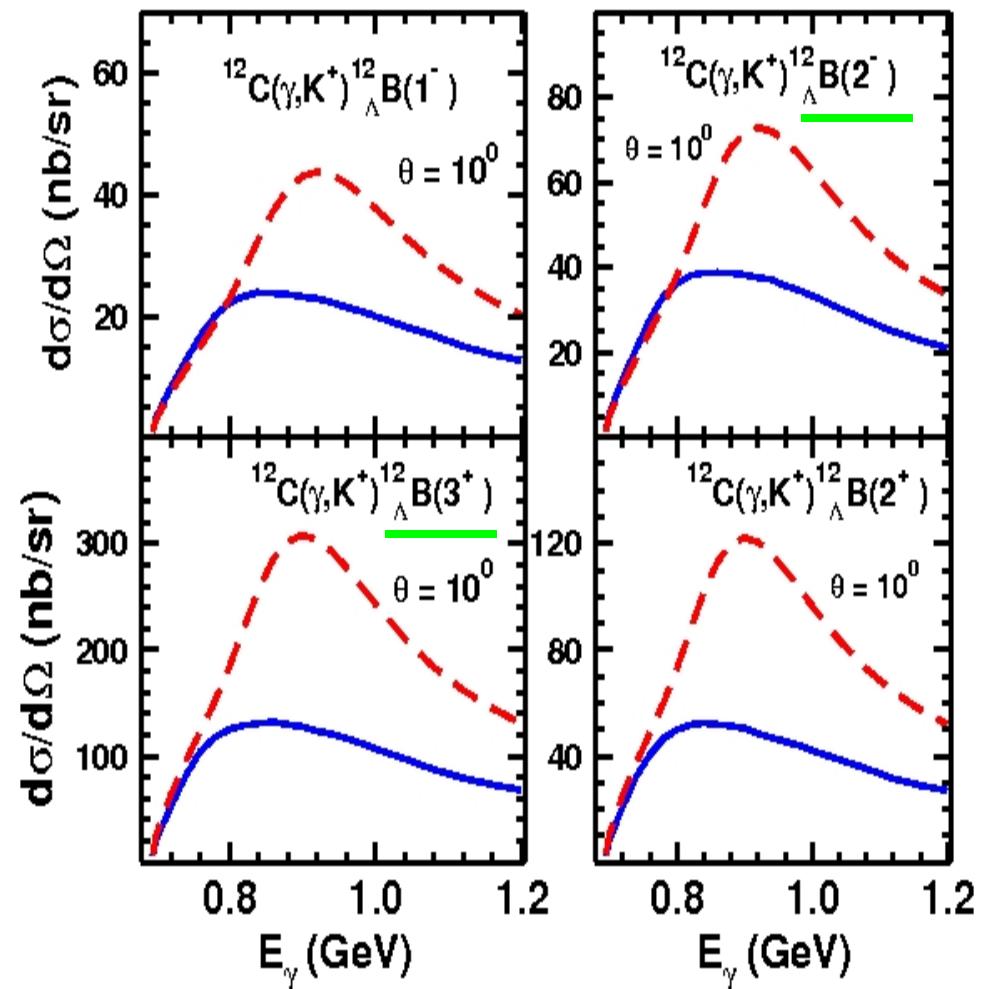
$2^+, 3^+ \Leftrightarrow (1p_{3/2}, 1p_{3/2})$

(potentials!) \Rightarrow

Diracp (phenomenological)

QMC

$|q| \approx [1.4, 1.7] \text{ fm}^{-1}$



Summary: Hypernuclei photoproduction

1. First attempt to study photoproduction of Λ -hypernuclei ($^{12}\text{C}(\gamma, \text{K}^+)_{\Lambda}^{12}\text{B}$ reaction) via quark-based model (QMC)
2. $d\sigma/d\Omega$ at Kaon angle $\theta = 10^\circ$ shows distinguishable difference!
3. Back ground inclusion for higher energies
4. Heavier hypernuclei?

Discussions, outlook

1. Study of Ξ -hypernuclei



2. Elementary $K^- p \rightarrow \Xi K^+$ reaction
3. Heavier Λ -hypernuclei photoproduction
4. Electroproduction of Λ -hypernuclei

Bound Nucleon GPDs and Incoherent DVCS

V. Guzey, A.W. Thomas, KT

arXiv:0806.3288 [hep-ph],

to be published in PLB

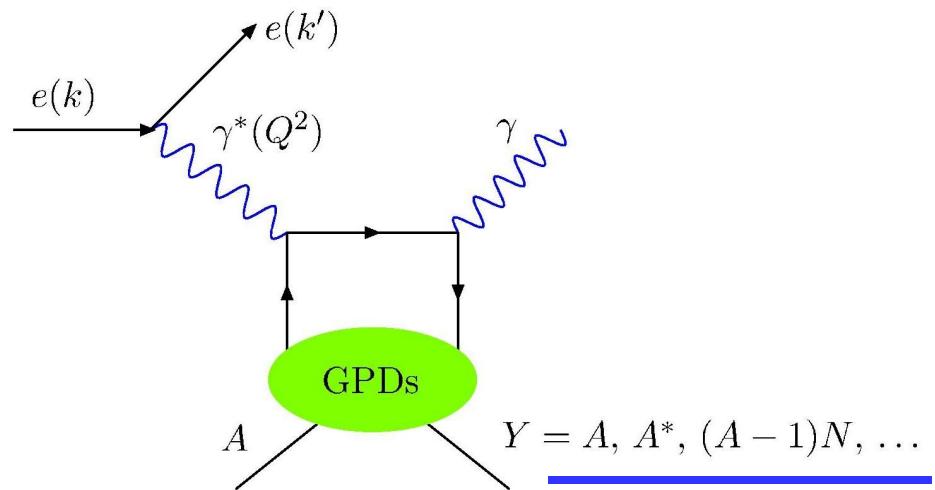
Medium effect on Generalized Parton Distributions

→ Deeply Virtual Compton Scattering

on a ^4He nucleus

Introduction

Deeply Virtual Compton Scattering (DVCS) is the cleanest example of hard exclusive process.



The QCD factorization theorem for hard exclusive reactions (DVCS, electroproduction of mesons) allows to interpret the measurements in terms of universal generalized parton distributions (GPDs) of the target.

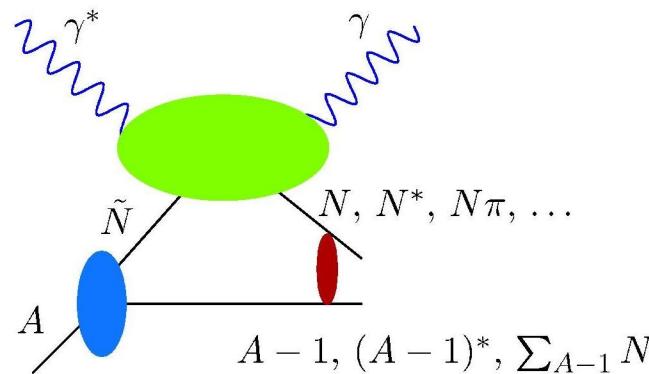
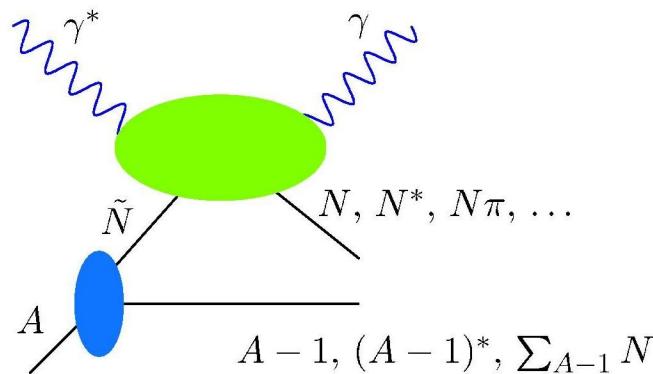
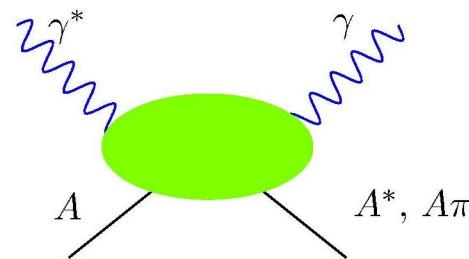
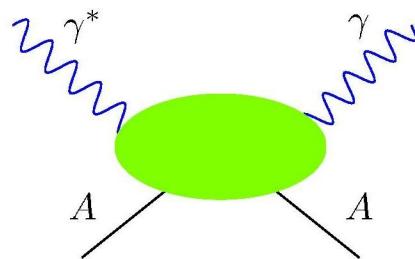
The GPDs generalize and interpolate between form factors and structure functions and encode information on 3D distributions of quarks and gluons in the target.

S on nuclear targets is more complex and versatile than DVCS on the free nucleon since:

any more final states can be excited

the reaction mechanism is more complex

different spin and isospin of the target are available.



Important roles of nuclear DVCS:

Nuclear DVCS gives the information on the nucleon GPDs complimentary to DVCS in the free proton:

- theoretical description of nuclear GPDs requires GPDs of the (bound) proton and neutron as input

VG and Strikman '03, VG '08; S. Scopetta '04; S. Liuti and S.K. Taneja '05

- incoherent DVCS on deuteron accesses almost-on-shell neutron GPDs

M. Mazouz *et al.* (Hall A), Phys. Rev. Lett. **99**, 242501 (2007)

- DVCS on polarized ^3He will probe GPDs of the neutron

- electroproduction of pseudoscalar mesons on deuteron is sensitive to non-pole contribution to the GPD \tilde{E}

F. Cano and B. Pire, Eur. Phys. J. A **19**, 423 (2004)

↓ ???!!!

- electroproduction of pseudoscalar mesons on ^3He at small t probes GPDs of the neutron ($\gamma_L^* + ^3\text{He} \rightarrow \pi^0 + ^3\text{He}$) or proton ($\gamma_L^* + ^3\text{He} \rightarrow \pi^+ + ^3\text{H}$)

L. Frankfurt *et al.*, Phys. Rev. D **60**, 014010 (1999)

ear DVCS is interesting in its own right:

light access novel nuclear effects not present in DIS and elastic scattering on nuclear targets:

contribution of non-nucleon (meson) degrees of freedom to the real part of the DVCS amplitude

M.V. Polyakov, Phys. Lett. B **555**, 57 (2003); VG and M. Siddikov, J. Phys. G **32**, 251 (2006)

unexpected pattern of nuclear shadowing for the real part of the DVCS amplitude at high-energies

A. Freund and M. Strikman, Phys. Rev. C **69**, 015203 (2004)

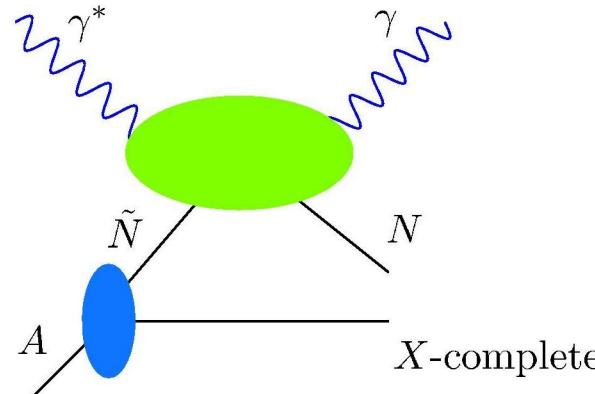
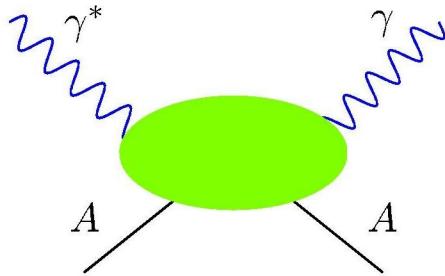
Will put stringent constraints on theoretical models of the nuclear structure:
covariant description is more important than for nuclear DIS and nuclear form factors

At high energies, nuclear DVCS is more sensitive to the physics of high parton densities and the parton saturation than inclusive scattering

.V.T. Machado, arXiv:0810.3665 [hep-ph]

Incoherent and coherent nuclear DVCS

Theoretical analysis of nuclear DVCS, the analysis is simplest when the final state is complete: elastic or complete set of final nuclear states.



Coherent nuclear DVCS:

- dominates at small t
- $\mathcal{A} \propto A F_A(t)$

Incoherent nuclear DVCS:

- dominates at large t
- $\mathcal{A} \propto F_N(t)$

In the final nuclear state is not detected (summed over), both coherent and incoherent contributions are present.

S amplitude: $\mathcal{T}_{\text{DVCS}}^A = -\bar{u}(k')\gamma_\mu u(k)\frac{1}{Q^2}\mathbf{H}^{\mu\nu}\epsilon_\nu^*$

ronic tensor: $\mathbf{H}^{\mu\nu} = -\int d^4x e^{-iqx}\langle \mathbf{X}|T\{J^\mu(x)J^\nu(0)\}|A\rangle \equiv \langle \mathbf{X}|\mathcal{O}(q)|A\rangle$

S amplitude squared:

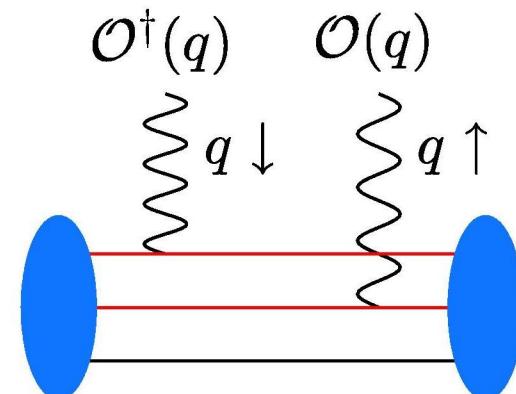
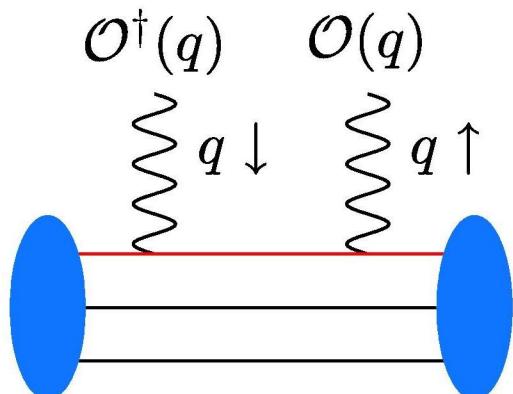
$$|_{\text{CS}}|^2 \propto \langle A|\mathcal{O}^\dagger(q)|\mathbf{X}\rangle\langle\mathbf{X}|\mathcal{O}(q)|A\rangle = \langle A|\mathcal{O}^\dagger(q)\mathcal{O}(q)|A\rangle$$

$$= \sum_{i,j} \langle A|\mathbf{N}_i\rangle\langle\mathbf{N}_i|\mathcal{O}^\dagger(q)\mathcal{O}(q)|\mathbf{N}_j\rangle\langle\mathbf{N}_j|A\rangle$$

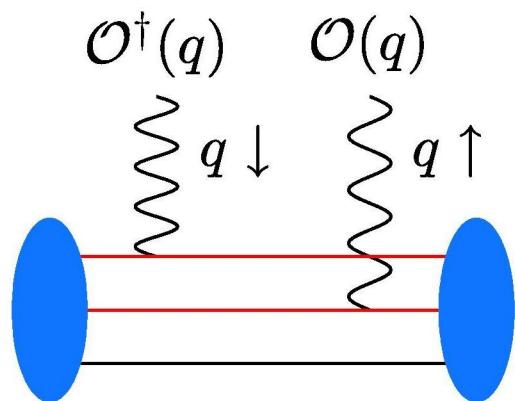
$$= \underbrace{\sum_i |\langle A|N_i\rangle|^2 \langle N_i|\mathcal{O}^\dagger(q)\mathcal{O}(q)|N_i\rangle}_{\text{red line}} + \underbrace{\sum_{i\neq j} \langle A|N_i\rangle\langle N_i|\mathcal{O}^\dagger(q)\mathcal{O}(q)|N_j\rangle\langle N_j|A\rangle}_{\text{green line}}$$

$$= \mathbf{A}|\mathcal{T}_{\text{DVCS}}^N|^2 + \underline{\mathbf{A}(\mathbf{A}-1)F_A^2(t' = A/(A-1)t)}|\mathcal{T}_{\text{DVCS}}^{A,\text{coh.enr.}}|^2$$

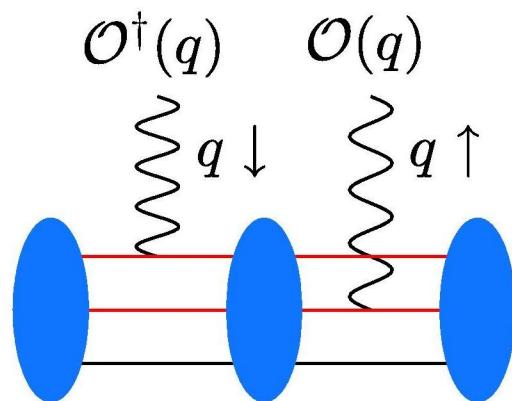
nkfurt, G.A. Miller and M.Strikman, Phys. Rev. D **65**, 094015 (2002)



the difference between the **coherent-enriched** and purely **coherent** contributions



$$A(A - 1)F_A^2(t')$$



$$A^2 F_A^2(t)$$

ral important comments:

he assumption of the completeness of final nuclear states (closure approximation) justified at sufficiently large t so that many final states are possible.

Both incoherent and coherent nuclear DVCS take place on medium-modified, off-shell nucleons that are subject to Fermi motion.

or incoherent nuclear DVCS:

$$\textcolor{violet}{A}|\mathcal{T}_{\text{DVCS}}^N|^2 \rightarrow \int_{\alpha_{\min}}^1 \frac{d\alpha}{\alpha} \rho_A^N(\alpha) |\mathcal{T}_{\text{DVCS}}^{N*}(\xi_N(\alpha))|^2$$

In my numerical results shown below, these effects are neglected. I only distinguish between protons and neutrons:

$$\underline{A}|\mathcal{T}_{\text{DVCS}}^N|^2 = \textcolor{blue}{Z}|\mathcal{T}_{\text{DVCS}}^p|^2 + \textcolor{blue}{N}|\mathcal{T}_{\text{DVCS}}^n|^2$$

$$A\mathcal{T}_{\text{DVCS}}^{A,\text{coh.enr.}} = \textcolor{violet}{F}_A(t') (\textcolor{blue}{Z}\mathcal{T}_{\text{DVCS}}^p + \textcolor{violet}{N}\mathcal{T}_{\text{DVCS}}^n) \equiv \textcolor{violet}{A}F_A(t') \mathcal{T}_{\text{DVCS}}^{N/A}$$

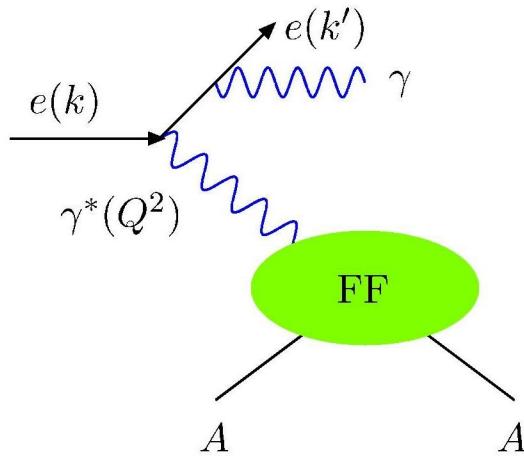
S cross section at the photon level (keeping only the GPD H):

$$\frac{d\sigma}{dt} \approx \frac{\pi \alpha_{\text{em}}^2 x_B^2}{Q^4} [A(A-1)F_A^2(t')|\mathcal{H}_{N/A}|^2 + Z|\mathcal{H}_p|^2 + N|\mathcal{H}_n|^2]$$

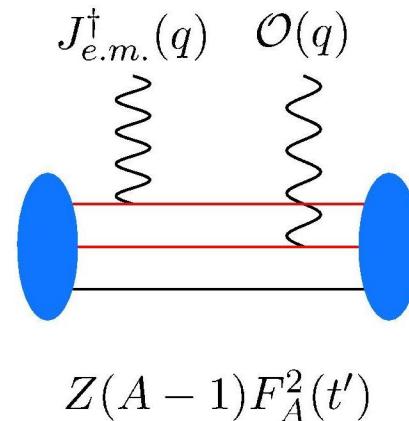
S beam-spin asymmetry $A_{LU}(\phi)$:

$$A_{LU}(\phi) = \frac{\vec{\sigma} - \overleftarrow{\sigma}}{\sigma^{\text{unp}}} = \frac{(A-1)Z F_A^2(t') \Delta \mathcal{I}_{N/A} + Z \Delta \mathcal{I}_p + N \Delta \mathcal{I}_n}{Z(Z-1) F_A^2(t') |\mathcal{T}_{N/A}^{\text{BH}}|^2 + Z |\mathcal{T}_p^{\text{BH}}|^2 + N |\mathcal{T}_n^{\text{BH}}|^2 + \dots}$$

e-Heitler process



"Counting" for coherent-enriched interference



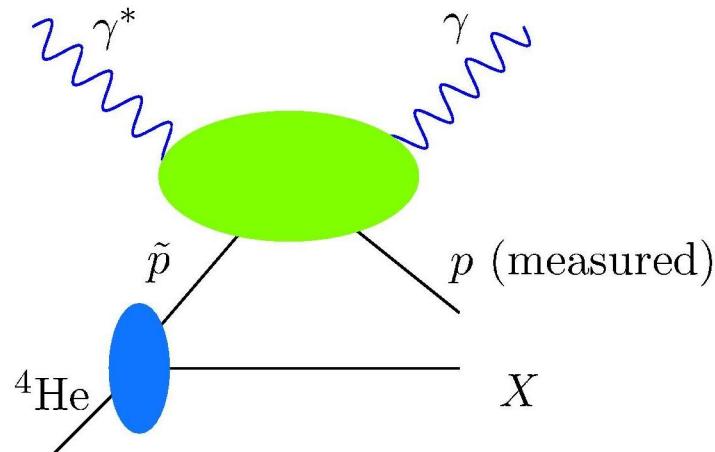
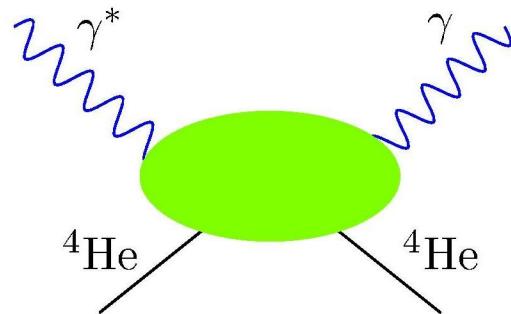
Medium modifications and incoherent nuclear DVCS

new Jefferson Lab (CLAS collaboration) experiment on DVCS on ${}^4\text{He}$ will measure

Agianyan, F.-X. Girod, K. Hafidi, S. Liuti, E. Voutier *et al.*, Jefferson Lab Experiment E08-024
)

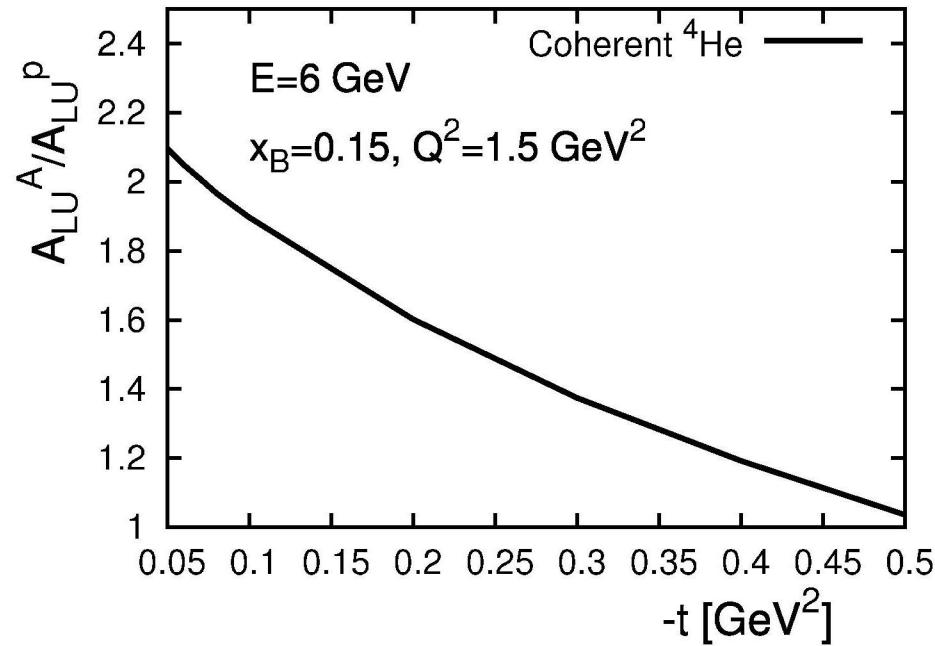
purely coherent DVCS on ${}^4\text{He}$ (the final nucleus will be detected using BoNuS detector)

coherent DVCS on the bound proton (the final proton is detected)



ictions for A_{LU}^A/A_{LU}^p for coherent DVCS on ${}^4\text{He}$ ($\phi = 90^\circ$)

uzey, Phys. Rev. C **78**, 025211 (2008)



ictions for the incoherent DVCS on bound proton in ${}^4\text{He}$

$$\frac{A_{LU}^{p^*}}{A_{LU}^p} = 1$$

However !! \Rightarrow

Fermi motion, off-shellness and medium-modification effects are not taken into account.

included the effect of medium-modifications of the bound nucleon assuming that medium nucleon GPDs are modified in proportion to the bound nucleon elastic factors.

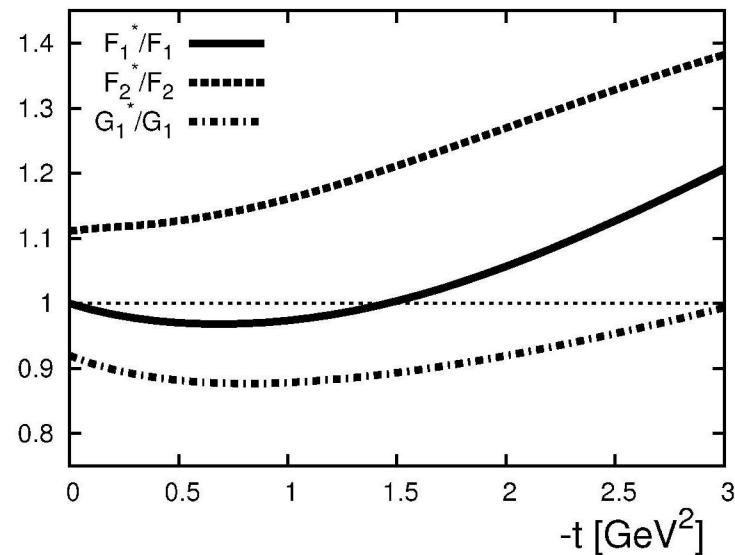
A.W. Thomas and K. Tsushima, arXiv:0806.3288

Model, assumption !

$$H^{q/p^*} = \frac{F_1^{p^*}(t)}{F_1^p(t)} H^{q/p}$$

$$E^{q/p^*} = \frac{F_2^{p^*}(t)}{F_2^p(t)} E^{q/p}$$

$$\tilde{H}^{q/p^*} = \frac{G_1^{p^*}(t)}{G_1^p(t)} \tilde{H}^{q/p}$$

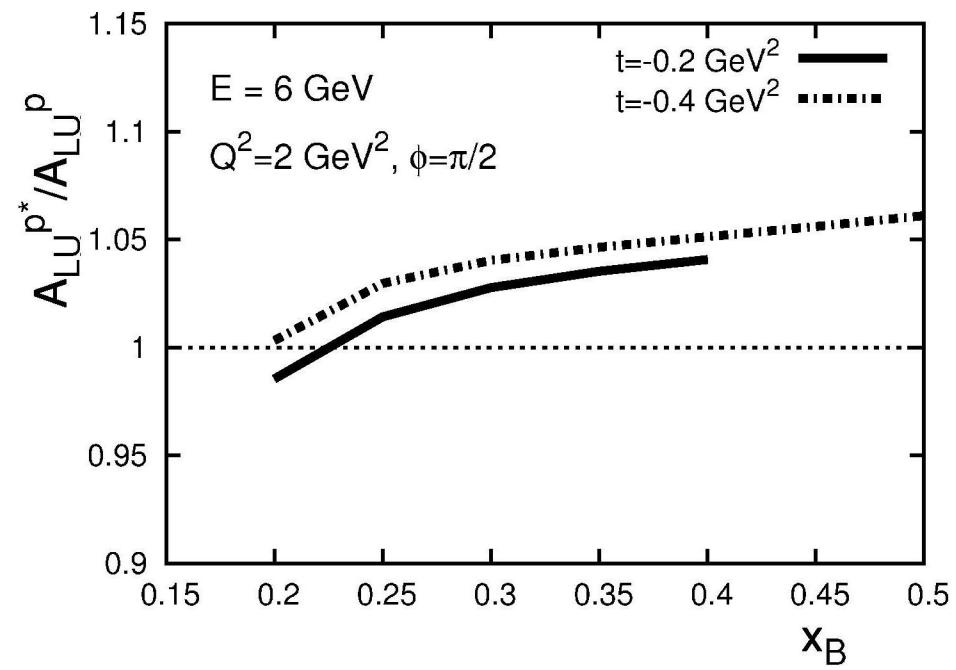
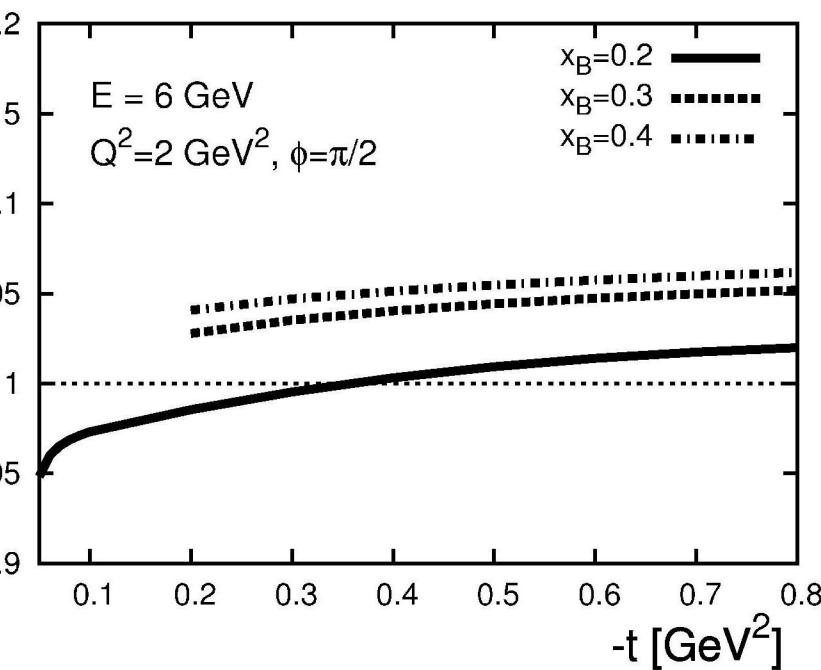


K. Saito, K. Tsushima and A.W. Thomas, Prog. Part. Nucl. Phys. **58**, 1 (2007)

medium-modified elastic form factors are taken from the Quark-Meson Coupling Model whose predictions are consistent with the polarization transfer measurement $e^- e' \vec{p})^3\text{H}$ (Hall A JLab): S. Malace, S. Strauch, arXiv:0807.2252 (Actually, MM+FM+FSI)

ictions for the ratio of the bound to free proton DVCS beam-spin asymmetries, $A_{LU}^p/A_{LU}^{p^*}$, for incoherent DVCS on ${}^4\text{He}$

A.W. Thomas and K. Tsushima, arXiv:0806.3288.



The deviation of $A_{LU}^{p^*}/A_{LU}^p$ from unity is as large as 6%

Our predictions are much smaller in size and different in shape (x_B -dependence) from the predictions of S. Liuti and S.K. Taneja, Phys. Rev. C **72**, 032201 (2005); C **72**, 034902 (2005)

Conclusions and Discussion

Using the completeness of the final nuclear states, one can derive an expression for nuclear DVCS that interpolates between the **coherent-enriched** and **incoherent** nuclear DVCS

For the coherent-enriched and purely coherent nuclear DVCS, we predict the "combinatoric" enhancement at small t , $A_{LU}^A/A_{LU}^p = 1.65 - 2$.

For the incoherent nuclear DVCS at large t , $A_{LU}^A/A_{LU}^p < 1$ due to the neutron contribution.

The effect of medium-modifications of the bound nucleon GPDs are modelled using results of the Quark-Meson coupling model; the deviation of $A_{LU}^{p^*}/A_{LU}^p$ is at most 6%.

In the above results, we neglected the effects of the Fermi motion and the final state interactions.

Future work (personal plans): final state interactions for incoherent DVCS on deuteron; DVCS on polarized ${}^3\text{He}$.

Speculations !!! (bound proton spin)

$$J_q + J_G = (\Delta q + L_q) + J_G = 1/2$$

- $g_A^* < g_A \rightarrow \underline{\Delta q^* < \Delta q}$
- $F_1^* \cong F_1 (F_1^*(0) = F_1(0) = 1), F_2^* > F_2$
 $\rightarrow \underline{Hq^* \cong Hq, Eq^* > Eq} (\mu p^* > \mu p)$

$$\underline{J_q^* = \frac{1}{2} - J_G^* = (\Delta q^* + L_q^*)}$$

$$\underline{= \frac{1}{2} \int dx x (Hq^* + Eq^*) > \frac{1}{2} \int dx x (Hq + Eq)}$$

$$\underline{= (\Delta q + L_q) - J_G = \frac{1}{2} - J_G = J_q}$$

$$\rightarrow \boxed{\underline{J_q^* > J_q} \quad (\underline{J_G^* < J_G} \text{ or } \underline{L_q^* > L_q})}$$